

# CC/SCC Outline

### Today!

- CCs
  - $\circ \qquad \text{Counting and finding the CCs}$
- SCCs
  - Counting and finding the SCCs: Trajan's Algorithm
- ChatGPT o.O
- Course policy updates

# Who's this guy?





- 4th year PhD student
- Researching Quantum Game Theory!
   7th semester as the Instructor of CS211 CP1
- Love to climb, hike 14ers (Colorado), read, ski, play board games, and yes, I love to code
- I have 2 doges :)
- Oh, and I do research into CS Education + GenAI

Connected Component (CC)/ Strongly Connected Component (SCC)

## **Connected Components**

- In an undirected graph, a cycle is "a non-empty trail in which only the first and last vertices are equal"
- For undirected, slightly different term: Connected Component
  - More formally, a set of vertices are a *connected component* in a graph if any vertex in the set can be reached by any other vertex in the set by traversing edges.
- What are the connected components in this graph?
  - $\circ$   $\hfill$  All of the nodes are in the same connected component! (a, b, c, d e, f, g)
- What if we remove the edge (b, c)?
  - (a, b) and (c, d, e, f, g) are the 2 connected components
- What if we then remove the edge (e, d)?
  - $\circ$  ~ Nothing changes because we can still reach all of (c, d, e, f, g) via edges



## **Strongly Connected Components**

- AKA identifying cycles in a directed graph
- More formally, a set of vertices are a *strongly* connected component in a *directed* graph if any vertex in the set can be reached by any other vertex in the set by traversing edges.
- What are the strongly connected components in this graph?
  - $\circ$  (a), (b), (c, d, e, f), (g) <- why is G separate?
- What if we remove the edge (b, c)?
  - $\circ$  (a), (b), (c, d, e, f), (g) <- nothing changes!
- What if we then remove the edge (d, e)?
  - (a), (b), (c), (d), (e), (f), (g)





# Tarjan's Algorithm

- Finding SCCs in O(V+E) using only one DFS (Kosaraju's uses two DFSs, we won't be teaching it here)
- Basics are as follows:
  - We perform a DFS on every node if it hasn't already been visited (as all DFS-based algorithms start)
  - We keep a record of nodes that we've seen in our current DFS in a stack. Each SCC will be found based on when we visited certain nodes ("discovery index") and where we detected a cycle
- Implementation:
  - Each vertex v has:
    - A "<u>discovered</u>" index which numbers nodes in order of discovery
    - A "lowest link" value which represents the lowest-indexed node on the **stack** reachable from v's DFS subgraph, including itself
  - $\circ$   $\hfill We deal with the stack in the following way:$ 
    - When we enter an undiscovered node, we push it onto the stack
    - When we leave a node in DFS, we either
      - 1. <u>Keep it on the stack</u>, if V or something that V can reach (later in the stack) can reach something that came *before* V (and therefore *earlier* on the stack than V)
      - 2. <u>Remove it from the stack</u>, if nothing that came after V (i.e. V can reach it via DFS) can reach something earlier on the stack (implies a cycle since "something earlier" can reach V). We also remove everything that V can reach from the stack (which would be later in the stack)
    - Therefore, V must be left on the stack if v.lowestLink < v.index, and removed if v.lowestLink == v.index

## **Pseudocode: Tarjan's Algorithm**

```
function strongconnect(v):
                                                                                     input: graph G = (V, E)
  v.index := index
                                                                                     output: set of strongly connected
  v.lowlink := index
                                                                                            components (sets of vertices)
  index := index + 1
  S.push(v)
                                                                                     index := 0
  v.onStack := true
                                                                                     S := empty stack
                                                                                     for each v in V do
  for each (v, w) in E do
                                                                                        if v.index is undefined then
       if w.index is undefined then
                                                                                            strongconnect(v)
                                                                                        end if
          strongconnect(w)
          v.lowlink := min(v.lowlink, w.lowlink)
                                                                                     end for
      else if w.onStack then
          v.lowlink := min(v.lowlink, w.index)
       end if
  end for
  if v.lowlink = v.index then
      start a new strongly connected component
      Repeat
          w := S.pop()
          w.onStack := false
          add w to current strongly connected component
      while w \neq v
      output the current strongly connected component
  end if
end function
```

DFS	Stack	node: (index, lowlink)
Explore a	(a)	a: (0, 0)
Explore b**	(a, b)	b: (1, 1)
Explore c	(a, b, c)	c: (2, 2)
Explore d	(a, b, c, d)	d: (3, 3)
Explore g**	(a, b, c, d, g)	g: (4, 4)
Done @g	(a, b, c, d)	SCC++: {g}
Explore e	(a, b, c, d, e)	e: (5, 5)
Explore f**	(a, b, c, d, e, f)	f: (6, 6)
Find d		f: (6, 3)
Done @f	(a, b, c, d, e, f)	e: (5, 3)
Find c		e: (5, 2)
Done @e	(a, b, c, d, e, f)	d: (3, 2)
Done @d	(a, b, c, d, e, f)	



DFS	Stack	node: (index, lowlink)
Done @c	(a, b)	SCC++: {f, e, d, c}
Done @b	(a)	SCC++: {b}
Find e		(Ignore, not on stack)
Done @a	()	SCC++: {a}

Leave f on the stack because it points to d

\*\*Node visit preference is arbitrary (and a bit contrived) here for academic purposes

## **Another animation**



### Graph algorithm resources

Play with algorithms here: <u>https://visualgo.net/en</u>

# **GPT of the Chat Variety**

## **GenAl Uses**

What is it good for?

#### What about in education?

- Conceptual questions
- Personal tutor
- Generating practice questions and test cases
  - https://chat.openai.com/share/c7b2acfc-9bf1-4202-95e1-544eab7fcc0c
- Re/writing/drafting/narratives/motivating examples

### Educational no-nos?

- Asking homework questions or project questions without understanding the topics
- Believing everything it says (confidence in mistakes)
  - https://chat.openai.com/share/20de44cb-7c29-47a1-88ce-db77e923c312
  - If you can't figure out why this is wrong, see the notes on this slide

## **Personal tutor?**

We would strongly encourage you to use the tools with phrases as follows:

- Help me with X, don't give me all the answers but help lead me to it
- <u>Provide suggestions for how to start</u> without solving my problem
- Find my bug but don't tell me exactly where it is, help me discover it for myself
- <u>Only give me a partial solution</u> to my problem, don't give it all away but guide me to the answer
- Here's my problem, <u>help me find the issue by asking me guiding questions only</u>

# How can we use GenAI well?

## Perspective: Interaction with the tools

Clear, concise, and specific

- 4-6 year old child
- Converse as you would with a human
  - "the part about X wasn't very clear, could you explain it differently, please?"
  - Language model

Expect imperfection, frequently

- Ask for 10 things, expect 2-4 that match requirements

# Prompt ~ Engineering~ (for educational purposes)

#### 1. Context

- a. Expert(s) to act as (persona prompt pattern)
- b. Setting
  - i. "Act as a political science professor teaching a summer school for gifted high school students"
  - ii. "Act as a political science professor teaching a summer school for academically advanced high school students"
- c. Audience base knowledge
- d. Together: "act as a collegiate professor with a PhD in Computer Science for a sophomore level data structures and algorithms course. Students are familiar with java."
- 2. Specific, measurable request: "give me a set of 10 problems to practice implementing Huffman Coding."
- > 2.5 Goals (optional if not simple or not short enough)

## Interacting with the response

- Most importantly: it is a *chat*bot
- Communicate likes and dislikes
- Separate specific refinements into individual queries
  - Do not say "Make 2 sound more like a story, make 3 clearer in the prompt, make 4 harder."
  - "Context bleeding"
- (sometimes) Remind it of the context
  - (if needed) Start a new chat, remind it of where you were

# Your turn! [pair programming]

In your pairs, choose one of the three following options. I will call on groups to share what they did/what mistakes they saw.

- 1. Have it create a tarjan's example, run through the steps, spot its mistakes
- 2. Create exam practice problems for Tarjan's algorithm with answers, critique either the question or the answer (or both)
- 3. Create practice problems for writing pseudocode on a topic from this semester, using one of the algorithms you've been taught (I've been told you're bad at that)
- These are not meant to be hard nor big tasks, just have fun with it.
  - Interaction
    - Be clear, concise, and specific
    - Converse with it (communicate likes and dislikes)
    - Expect imperfection
    - (sometimes) start a new chat/remind context

#### • Prompt engineering techniques

- Context ("act as," setting, base knowledge)
- Specific, measurable request
- (sometimes) Goals

# Can I use ChatGPT on my homework to get answers?

No\*T

\*This week you will be required to use GenAI to generate a solution for you to critique on <u>ONE (1)</u> problem only.

<sup>T</sup>We encourage you to seek tutoring help and help with conceptual questions, using GenAI without copying from it.

# Course Policy Updates (pay close attn)

### Nothing changes

- 1. If you copy + paste from AI (or anywhere), it is STILL cheating.
  - a. Specifically, if you submit work which is not your own, it is plagiarism in accordance with the course syllabus.
- 2. We will still evaluate correctness, so be careful if you use the tools for help.
- 3. You will not have these tools on the exams, so prepare yourself accordingly!
- 4. You are still 100% responsible for your responses. You are NOT allowed to complain if AI gave you something wrong.

### HW6-AI

- 2 problems, required to use GenAl only
- Participation in all 3 components (prelab + 3 surveys, this lecture, HW6-AI + 3 surveys) will get you full points for an extra homework assignment (basically for free)
  - Available today, have 1 week

### What did we learn today?

- Graphs! Cycles! Directed vs undirected, connected and strongly connected components
- Difference between CC and SCC?
  - SCC is for directed graphs, CC for undirected
- How do we find CCs?
  - Everything reachable from the current node DFS or BFS, take your pick
- How do we find SCCs?
  - Tarjans DFS once using a stack to keep track of what's in the current SCC
- How should you interact with chat-based GenAI?
  - Be clear, concise, and specific
  - Converse with it
  - Expect imperfection
  - o (sometimes) remind it of the context or even start a new chat
- Prompt engineering techniques?
  - Context ("act as," setting, base knowledge)
  - Specific, measurable request
  - (sometimes) Goals
- What do Canadians call Canadian bacon in Canada?
  - In Canada, the term "Canadian Bacon" is not used. The cut of meat from the loin is referred to as "back bacon". In Southern Ontario, "Peameal Bacon", as it is referred to there, is a similar product; however it is not smoked but rather set in a brine.
- How tall is the tallest person in the world?
  - The tallest man living is Sultan Kösen (Turkey, b.10 December 1982) who measured 251 cm (8 ft 3 in) in Ankara, Turkey, on 08 February 2011. The part-time farmer was the first man over 8 ft (2.43 m) to be measured by Guinness World Records in over 20 years.

# End of CC/SCC lecture